



Hooke's law:

$$F_s = -kx \quad (1)$$

where

k - spring constant,

x - extension of the spring (position of the ball).

Gravitational force:

$$F_g = mg \quad (2)$$

$$x = x_0 \cos(\omega t), \quad (3)$$

$$x' = -\omega x_0 \sin(\omega t), \quad (4)$$

$$x'' = -\omega^2 x_0 \cos(\omega t). \quad (5)$$

where

x_0 - amplitude of oscillation,

ω - period of oscillation,

t - time.

combining (3) and (5):

$$a = -\omega^2 x \quad (6)$$

Newton's second law then gives us:

$$F = ma, \tag{7}$$

$$-kx = -m\omega^2x, \tag{8}$$

$$\omega = \sqrt{\frac{k}{m}}. \tag{9}$$

Helpful formulas:

$$T = \frac{1}{f}, \tag{10}$$

$$\omega = \frac{2\pi}{T}. \tag{11}$$

Energies:

$$E_p = \frac{1}{2}kx^2, \tag{12}$$

$$E_k = \frac{1}{2}mV^2. \tag{13}$$

Damped oscillation equation:

$$x = x_0e^{-\gamma t}\cos(\omega t) \tag{14}$$